# Estimating co-patenting intensities between regions: some theoretical considerations

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#### Introduction

- The gravity model became a popular tool to examine research collaborations between regions.
  - see e.g. Maggioni et al., (2007); Broekel et al. (2014), Tóth et al. (2021)
- Most analyses lack a proper theoretical underpinning.
- Neglecting theory raises several questions:
  - How to specify the gravity model?
  - What should be considered as the "mass" of the region?
  - What to do with the zeros?
  - The model is not suitable for predicting

#### Core assumptions

- Researchers' human capital is the function of investment in own research and collaborations.
- Knowledge from different research collaborations are not perfect substitutes.
- Participants in collaborations face fixed and variable costs.
- Researchers do not form "joint research ventures".

#### Model

- Consider an economy with S regions and N identical researchers. Each region is inhabited by N(r) researchers.
- Researchers maximize consumption (income cost of R&D activity)
- Knowledge production:

$$h_i(r) = x_i(r)^{\rho} + \sum_{j \neq i}^{N(r)} X_{ij}(r)^{\rho} + \sum_{s \neq r}^{S} \sum_{j=1}^{N(s)} X_{ij}(r,s)^{\rho}$$

where

$$X_{ij}(r,s) = x_{ij}(r,s)x_{ji}(s,r)$$

 $r, s \in S$  region,  $i \in N(r)$  researcher.

#### Model

• Cost of a collaboration:

$$c_{ij}(r,s) = \kappa(r,s)x_{ij}(r,s) + f(r,s)$$

• Two researchers collaborate only if

$$w(r)X_{ij}(r,s)^{\rho} > x_{ij}(r,s)x_{ji}(s,r) + f(r,s)$$

applies for both parties.

#### Co-patenting intensity

• Solving the model, the knowledge created by researchers *i* and *j*:

$$X_{ij}^*(r,s) = \rho^{\frac{2}{1-2\rho}} \left( w(r)w(s) \right)^{\frac{1}{1-2\rho}} \kappa(r,s)^{-\frac{2}{1-2\rho}}$$

#### if

$$f(r,s) < (1-\rho)\rho^{\frac{2\rho}{1-2\rho}} \left(w(r)w(s)\right)^{\frac{1}{2(1-2\rho)}} \kappa(r,s)^{-\frac{2\rho}{1-2\rho}}$$

• 0 otherwise!!!

The lack of patents between two regions means that it is not profitable collaborate. → selection

## Consequences

- What is the mass of the region?
  - wages w(r) and number of researchers N(r)
- Selection bias is introduced into the gravity model when regions pairs with zero joint patents are excluded!
  - Selection into interregional collaborations should be estimated first!
- What predicts participation in interregional R&D collaborations?
  - wages w(r),  $\kappa(r,s)$  and f(r,s)
  - Suppose that  $\kappa(r,s)$  depends on geographical distance. If we want to estimate distance decay, omitting zeros or misspecifying the selection equation ( $\kappa(r,s)$  is not included) estimates will be biased.
  - Co-patenting intensities and selection are both a function of researchers' wages!

## Consequences

- What happens if the fixed cost, of collaborations is reduced? f(r,s)
  - e.g. support networking, industrial trade meets, fairs
  - More region pairs will join (extensive margin)
- What happens if the variable cost of collaborations is reduced?  $\kappa(r,s)$ 
  - Since co-patenting intensities and selection are both a function of variable costs,
    i) more region pairs will join (extensive margin)

ii) More patents may occur where collaborations are formed previously (intensive margin)

#### What next...?

- Estimate the model on EPO's Patstat data
- Consider different distance measures
- Recover model parameters
- Simulate the model



**Proximity:** inverse of physical distance between the centroids of region *i* and *j*.

**Cosine:** degree of overlap between the patent class portfolios of region *i* and *j*.



